

#### For Government Audits

 If a particular probability sample design is properly executed, i.e., <u>defining the universe</u>, <u>the frame</u>, <u>the</u> <u>sampling units</u>, using <u>proper randomization</u>, accurately measuring the <u>variables of interest</u>, and using the <u>correct</u> <u>formulas for estimation</u>, then assertions that the sample and its resulting estimates are "not statistically valid" cannot legitimately be made. In other words, a probability sample and its results are always "valid."

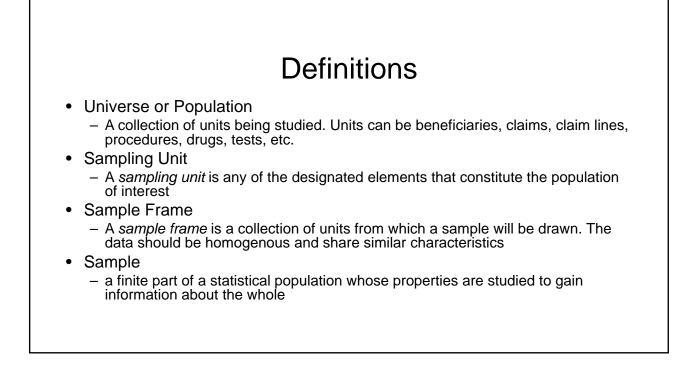
[CMS Pub.100-08 Chapter 3 Section 10.2]

#### For Self-Disclosure

- If the financial review was based upon a sample, the review report must also include the Sampling Plan that was followed. At a minimum, this includes:
  - Sampling unit
  - Sampling Frame
  - Sample Size
  - Source of Random Numbers
  - Method of Selecting Sampling Units
  - Sample Design
  - Missing Sample Items and Other Evidence
  - Estimation Methodology

#### The Sampling Process

- 1. Define the population of interest
- 2. Create a sampling frame
- 3. Determine the sampling method
- 4. Calculate the sample size
- 5. Sample the data
- 6. Analyze the results
- 7. Infer to the population of interest



#### Definitions

- Parameter
  - Considers the characteristics of the population
- Statistic
  - A numerical value, such as standard deviation or mean, that characterizes the sample from which it was derived
- EPSeM
  - Equal Probability of Selection Method
  - the application of a sampling technique that results in the population elements having equal probabilities of being included in the sample.



- Large enough to minimize sampling error and not so small that it no longer fairly represents the population in question
- Too large a sample can cost more money and consume more resources without added benefits
- Too small a sample creates too much error and renders the results useless

#### Ideally . . .

- The sample is representative of the qualities of the population
  - The sample has the same characteristics as the population
- It is of sufficient size to satisfy the assumptions of the statistical techniques used in our analysis
- NOTE: For self-disclosure, the sample size must be at least 100 claims (or other sampling units)

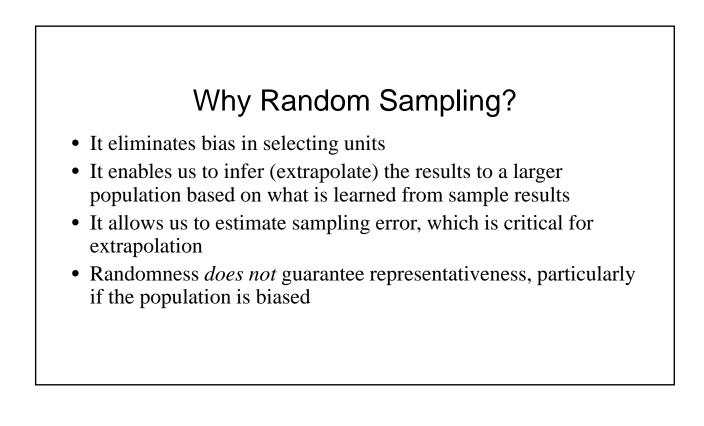


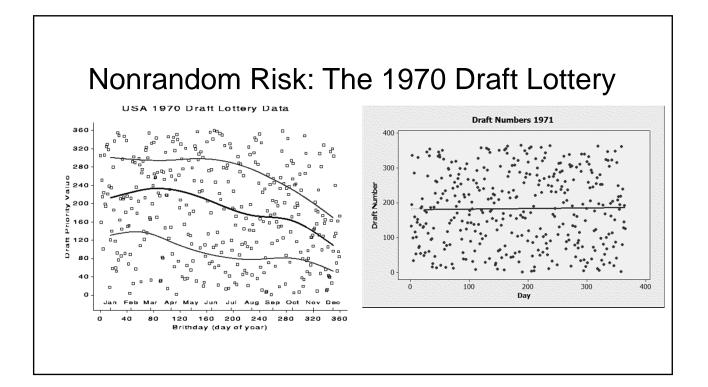
- Any probability sample will have some inaccuracy, or sample error
- The larger the sample, the smaller the error (not always a good thing)
- The more homogenous the variables, the smaller the error (always a good thing)
- Sample size determination is a fairly complex undertaking

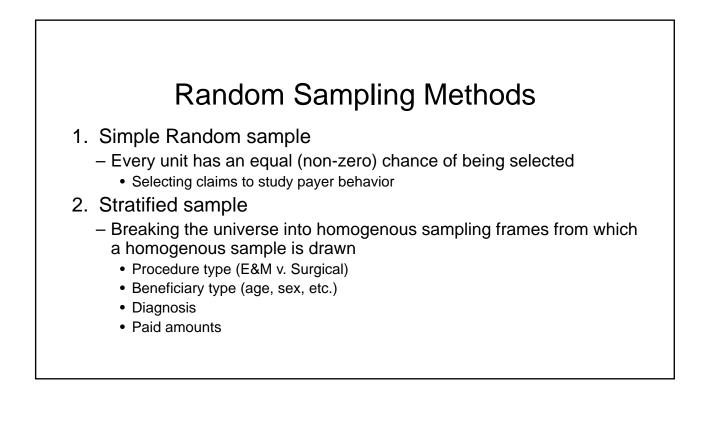
Low accuracy

#### Precision vs. Accuracy

- Accuracy measures how close the statistic is to the true value
- Precision measures how close the variables are to one another
- Accuracy is easier to fix; just move the model
- Precision is harder to fix as it is indicates instability

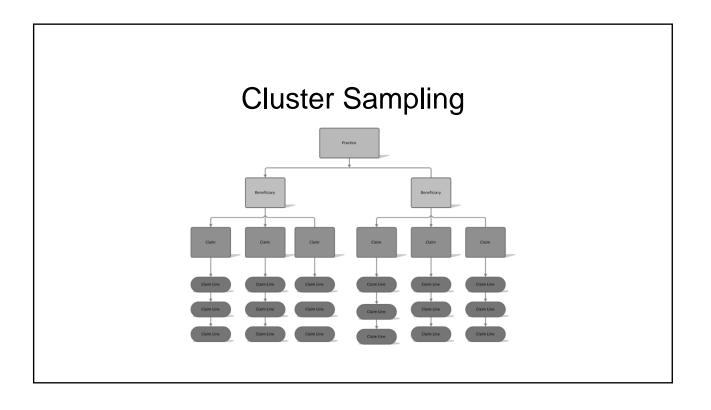






#### **Random Sampling Methods**

- 3. Cluster sampling
  - Organizes the units into similar subsets
  - Two stage
    - i.e., random sample of beneficiaries and then random sample of claims for each
  - Multi-stage
    - i.e., random sample of beneficiaries from which we draw a random sample of claims from which we draw a random sample of claim lines

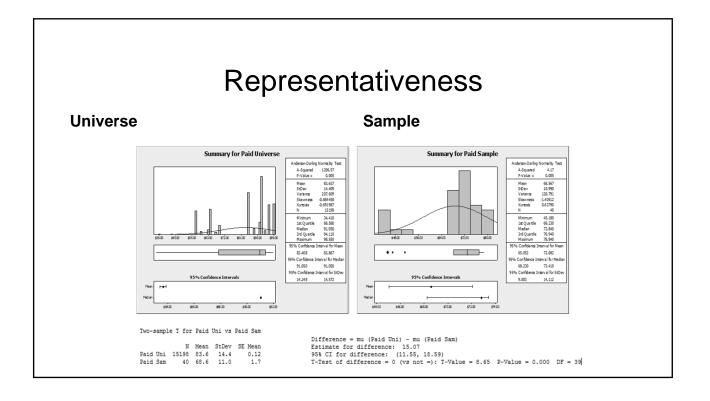


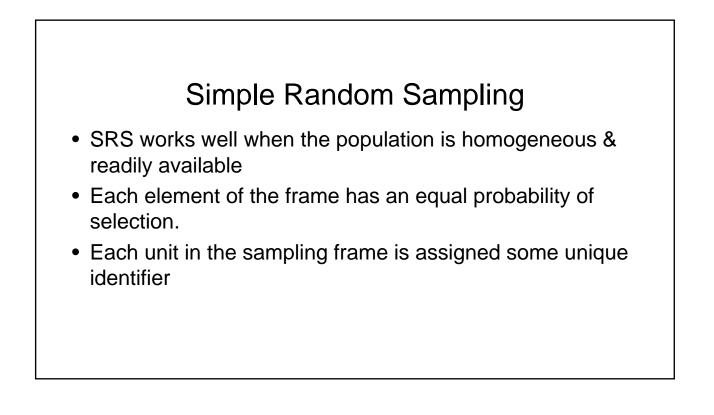
#### How Do I Randomize?

- You can use a software program
   RAT-STATS, MiniTab, Excel, SQL, etc.
- You can systematize the sample
   Every n<sup>th</sup> unit, such as every 10<sup>th</sup> or 25<sup>th</sup> or 50<sup>th</sup> unit
- You can sort by some variable (such as claim ID or claim code) that is not otherwise ordered

# How about Statistically Valid?

- There is a difference between a sample being random and it being statistically valid
- Random just means that every unit had an equal chance of being selected
- Statistically valid has to do with the representativeness of the sample





# Systematic Sampling

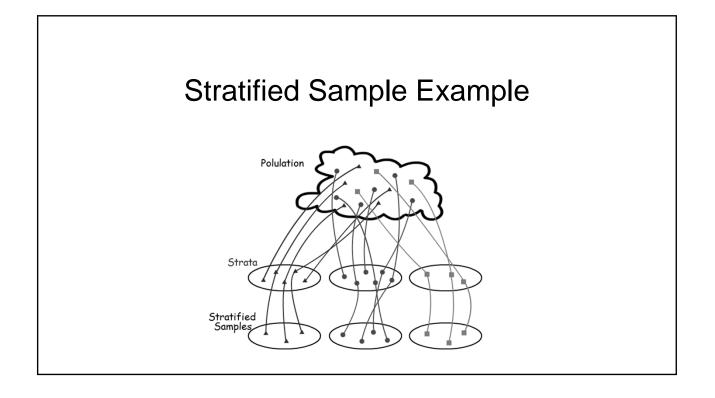
- First, arrange the sampling frame (or population) using some ordering technique and select at regular intervals

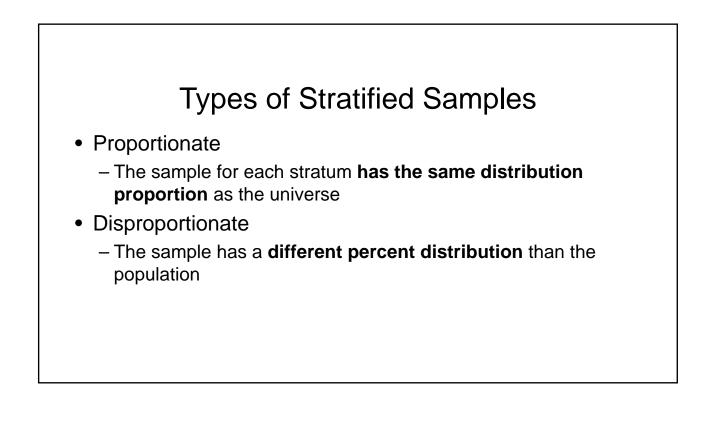
   i.e., every 4<sup>th</sup> or all odd or even
- Start from a random position

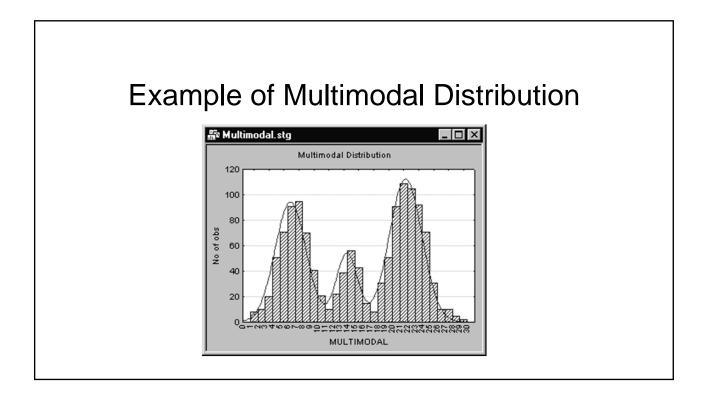


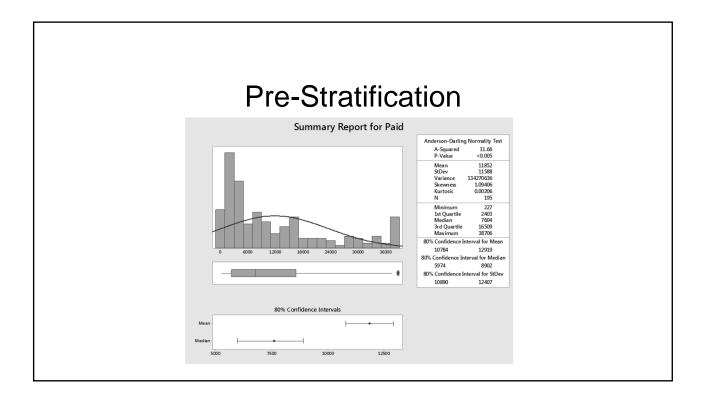
- When the population can be described by a number of different characteristic groups, the frame can be organized into separate "strata"
- Each stratum can then sampled as an independent subpopulation, subject to SRS
- Most often, the strata are sampled proportionate to the population
- If done properly, it reduces variability and increases precision

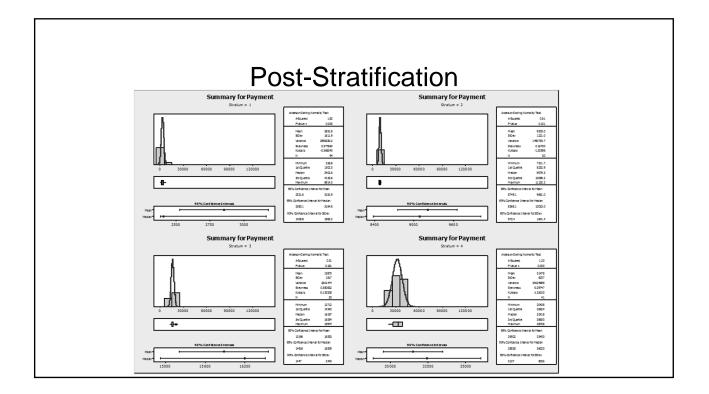
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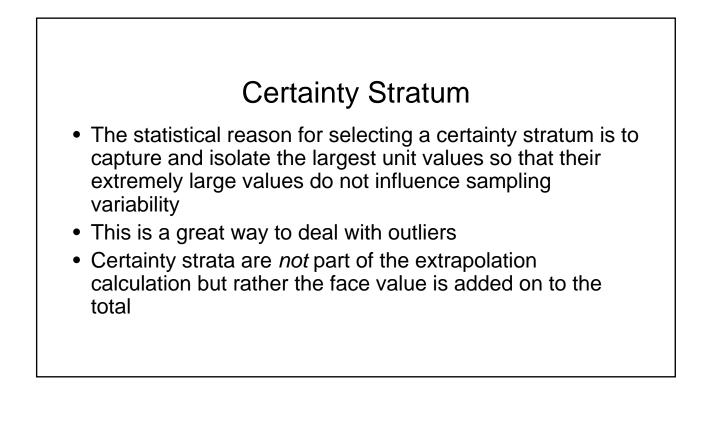






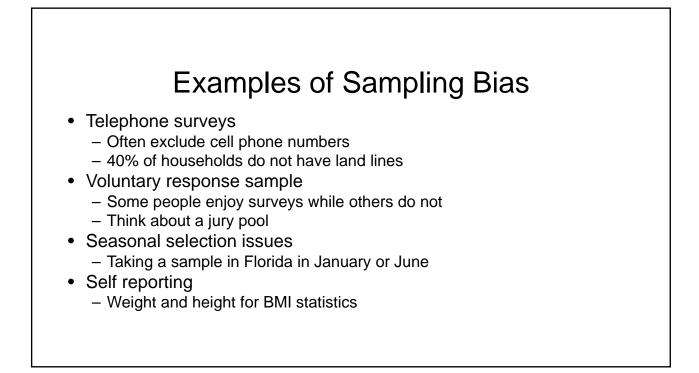






# Sampling Bias

- A sampling method is called *biased* if it *systematically* favors some outcomes over others.
- Any event that causes one or more variables within a population to have a different chance of selection
- This can lead to over or under representation of a group of variables
- Bias isn't always bad



## Types of Appraisal Methods

- Variable Appraisal
  - To measure a quantitative characteristic such as the dollar amount per claim, line or beneficiary
  - Continuous variable
- Attribute Appraisal
  - to determine the number of items that meet a given set of criteria, such as the proportion of lines with improper modifier usage
  - Proportion or ratio (like a percentage of error)

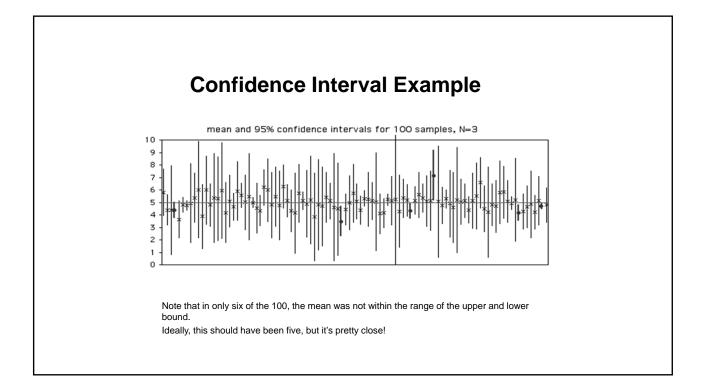
#### Sample Error

- Sample error is an estimate of the potential error (or precision) the results have in relation to the population (or universe)
- Most often, sample error is measured by confidence intervals

# What is a Confidence Interval (CI)?

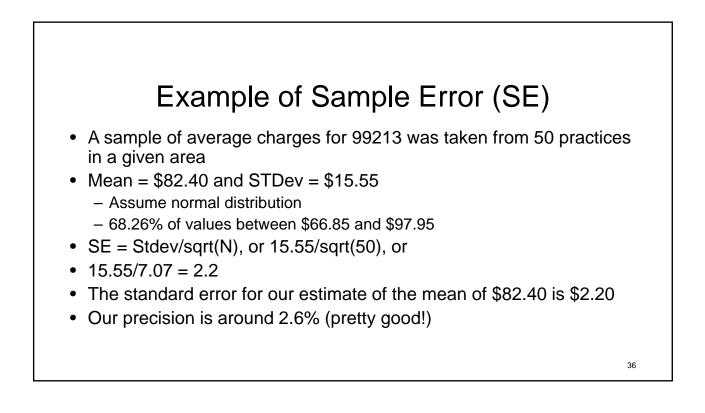
- The purpose of a confidence interval is to validate a point estimate; it tells us how far off our estimate is likely to be
- A confidence interval specifies a range of values within which the unknown population parameter may lie

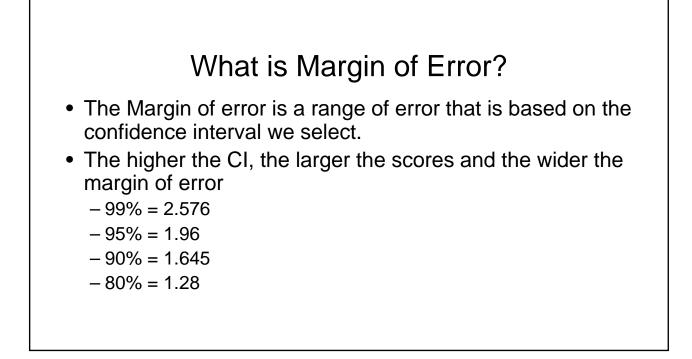
   Normal CI values are 90, 95%, 99% and 99.9%
- The width of the interval gives us some idea as to how uncertain we are about an estimate
  - A very wide interval may indicate that more data should be collected before anything very definite can be inferred from the data

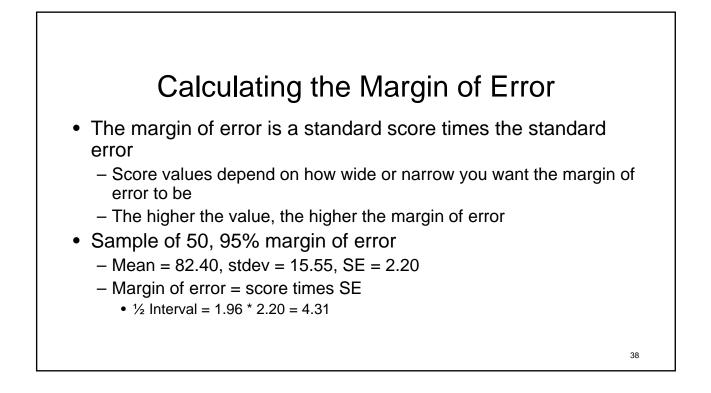


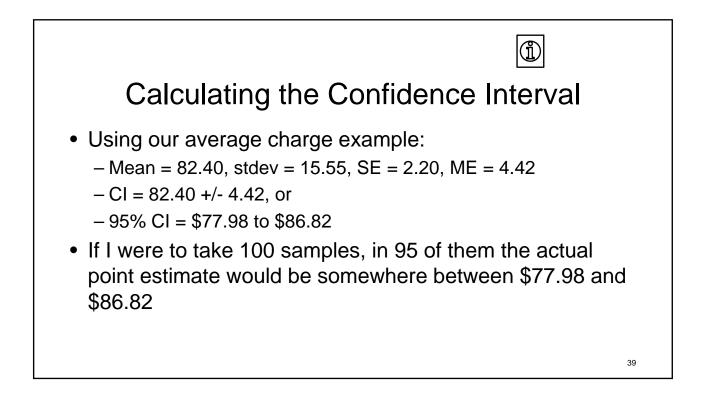
# Calculating Sample Error

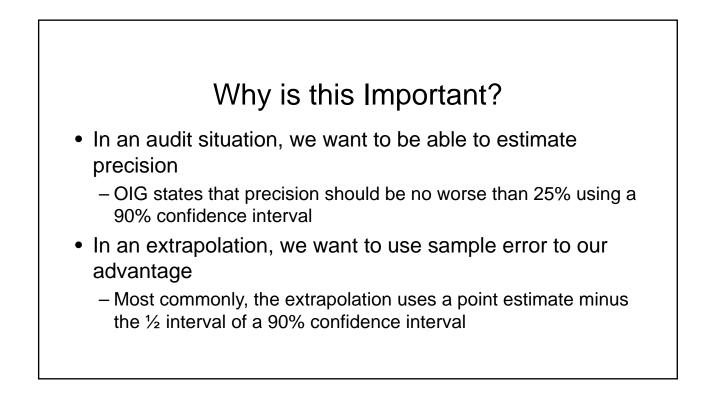
- For a variable appraisal, sample error is calculated as the standard deviation divided by the square root of the sample size
- For an attribute appraisal, sample error is calculated as the square root of the proportion times 1- proportion, all divided by the sample size





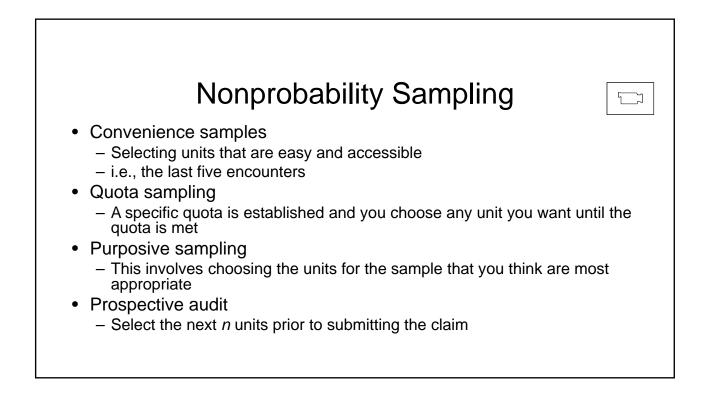






#### Creating a Sample for Review

- It is not necessary (and often ill-advised) to create a statistically valid random sample (SVRS) for an internal review
  - Obligates you to extrapolate the overpayments
- Use nonprobability sampling



# For More Information

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